

大同大學 97 學年度轉學入學考試試題

考試科目：離散數學

所別：資訊工程學系

第 1/2 頁

註：本次考試 不可以參考自己的書籍及筆記； 不可以使用字典； 不可以使用計算器。

Mark true(T) or false (F) for Questions 1-2. [8%]

1. The statement $p \rightarrow (q \rightarrow r)$ is equivalent to $(p \rightarrow q) \rightarrow r$.
2. The statement $(q \wedge (p \rightarrow \neg q)) \rightarrow \neg p$ is a tautology.

Multiple Choice Problems (3-9): each problem has *exactly one* correct choice.

3. In the questions below $P(x,y)$ means " $x + 2y = xy$ ", where x and y are integers. How many of these statements are TRUE? [8%]

$$\forall x \exists y P(x,y). \exists x \forall y P(x,y). \forall y \exists x P(x,y). \exists y \forall x P(x,y).$$

- (a) 0 (b) 1 (c) 2 (d) 3 (e) 4.

4. In the questions below, suppose $A = \{a,b,c\}$ and $B = \{b,\{c\}\}$. How many of these statements are TRUE? [8%]

$$\begin{aligned} c \in A - B. & \quad |P(A \times B)| = 64. \quad \{c\} \subseteq B. \\ \{a,b\} \in A \times A. & \quad \{b,\{c\}\} \in P(B). \quad \{\{\{c\}\}\} \subseteq P(B). \end{aligned}$$

- (a) 2 (b) 3 (c) 4 (d) 5 (e) 6

In the questions below suppose the variable x represents students, $F(x)$ means " x is a freshman", and $M(x)$ means " x is a math major". Match the statement in symbols with one of the English statements in this list: [16%]

- a. Some freshmen are math majors.
- b. Every math major is a freshman.
- c. No math major is a freshman.

5. $\neg \forall x (F(x) \rightarrow \neg M(x)).$

6. $\forall x (M(x) \rightarrow \neg F(x)).$

7. $\forall x (M(x) \rightarrow F(x)).$

8. $\exists x (F(x) \wedge M(x)).$

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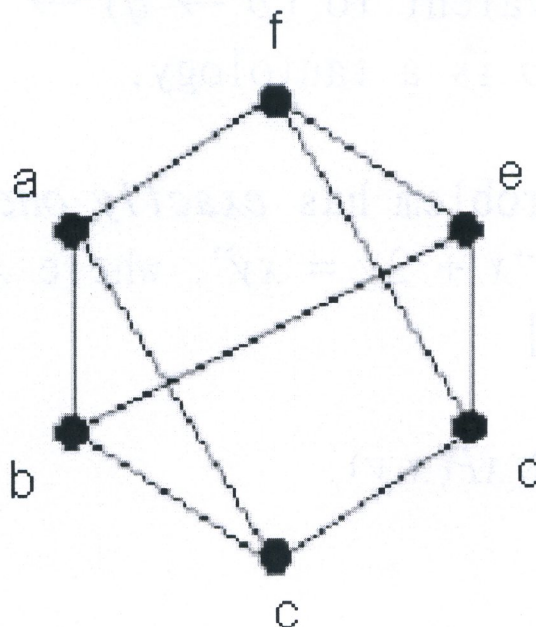
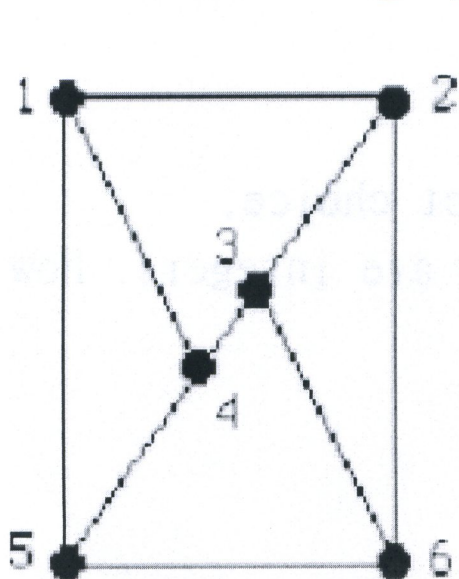
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第 2/2 頁

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Answer these questions in sufficient details.

9. Are these two graphs isomorphic? If so, label the corresponding vertex pairs. [12%]



| 1 | 2 | 3 | 4 | 5 | 6 |
|---|---|---|---|---|---|
| | | | | | |

In the expansion of $(1+x^2+x^4)^5$:

10. How many terms are there? [8%]

11. What is the coefficient of x^8 ? [4%]

The set $S = \{1,2,3,\dots,10\}$. Find the number of subsets of S satisfying each of the following conditions:

12. ... contains no odd numbers [4%]

13. ... contains exactly three elements, all of them even. [4%]

14. ... contains exactly five elements, the sum of which is even. [4%]

15. Solve the following recurrence relation: [12%]

$$a_n = 2a_{n-1} + 5, \quad a_0 = 3.$$

16. How many different channels are needed for six television stations (A,B,C,D,E,F)

whose distances (in miles) from each other are shown in the following table?

Assume that two stations cannot use the same channel when they are within 150 miles of each other? [12%]

| | A | B | C | D | E | F |
|---|-----|-----|-----|-----|-----|-----|
| A | — | | 175 | 100 | 50 | 100 |
| B | 85 | — | 125 | 175 | 100 | 130 |
| C | 175 | 125 | — | 100 | 200 | 250 |
| D | 100 | 175 | 100 | — | 210 | 220 |
| E | 50 | 100 | 200 | 210 | — | 100 |
| F | 100 | 130 | 250 | 220 | 100 | — |