

大同大學 100 學年度 轉學考試 試題

科目名稱: 微積分 系別: 各系所
註: 本次考試不可參考書籍及筆記

不可使用字典

共一頁
不可使用計算機

1. Evaluate the limits:(每小題8分)

(a) $\lim_{x \rightarrow 3} \frac{-x^2 + 5x - 6}{x - 3}$.

(b) $\lim_{x \rightarrow -2^+} \left(\frac{x^2 - 2}{x + 2} \right)$.

2. Find the derivatives $\frac{dy}{dx}$ of the following:(每小題8分)

(a) $y = e^x \tan x$.

(b) $y = x^{(1-x)}$.

(c) $\tan(x + y) = -2xy + y^2$.

3. For the equation $\sin x + \cos y = \sin x \cos y$, find $\frac{dy}{dx}$ and the equation of the tangent(切線) at $\left(0, \frac{\pi}{2}\right)$. (10分)

4. The edge(邊) of an ice cube(正方體) was found to be 30cm. Suppose that there was a possible error(誤差) in measurement(量測) of 0.1cm on the edge, what is the maximum possible error in computing the volume? (8分)

5. Find all extreme values of the function $f(x) = \int_0^x 1 + \sin t \, dt$ on the interval $[0, 2\pi]$. (8分)

6. Evaluate the following:(每小題8分)

(a) $\int \left(\frac{x}{4} - \frac{7}{x^2} + 4x^3 \right) dx$.

(b) $\int \frac{x + 2}{\sqrt{x^2 + 4x + 13}} dx$.

(c) $\int x \ln x \, dx$.

7. Find a power series (冪級數) for $f(x) = \cos^2(3x)$, centered at 0. (10分)